

Ex) Build a set of half-adder using:-

- Ⓐ NOR gate only.
- Ⓑ NAND gate only.

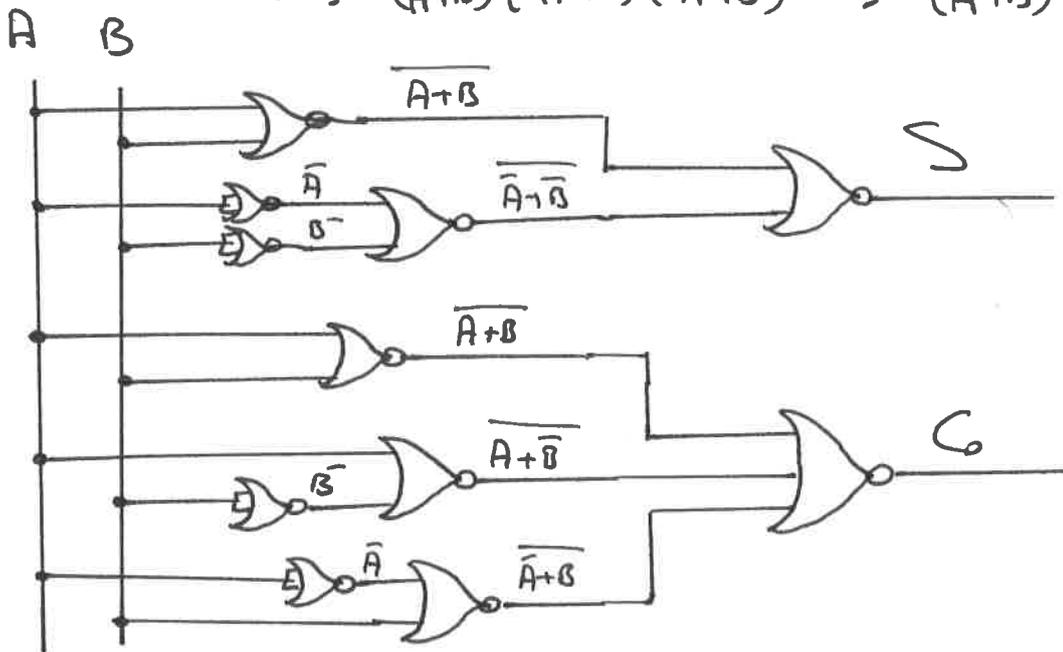
Ⓐ using NOR gate

$$S = \overline{(A+B)(\bar{A}+\bar{B})}$$

$$S = (A+B)(\bar{A}+\bar{B}) = \overline{\overline{(A+B)} + \overline{(\bar{A}+\bar{B})}}$$

$$C_0 = \overline{(A+B)(\bar{A}+\bar{B})(A+\bar{B})}$$

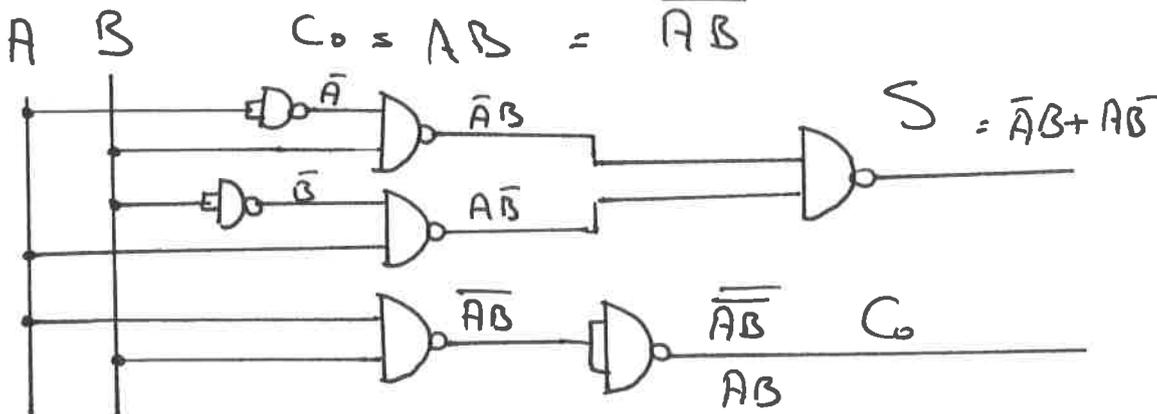
$$C_0 = (A+B)(\bar{A}+\bar{B})(A+\bar{B}) = \overline{\overline{(A+B)} + \overline{(A+\bar{B})} + \overline{(\bar{A}+\bar{B})}}$$



Ⓑ Using NAND gate

$$S = \bar{A}B + A\bar{B} = \overline{\overline{\bar{A}B} + \overline{A\bar{B}}} = \overline{A\bar{B}} \cdot \overline{\bar{A}B}$$

$$C_0 = AB = \overline{\overline{AB}}$$



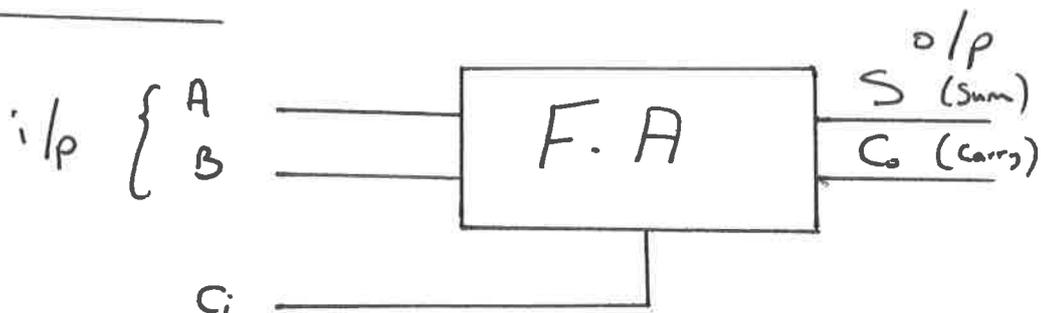
# Full Adders

A Full-adder is a combinational circuit that performs the arithmetic sum of three input bits. It consists of three inputs and two outputs.

Truth table :-

i/p			o/p	
A	B	C <sub>i</sub>	S	C <sub>o</sub>
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

Block Diagram



"Block diagram of Full-Adder (F.A)".

From truth table :-

$$S = \Sigma 1, 2, 4, 7$$

$$S = m_1 + m_2 + m_4 + m_7$$

$$= \bar{A}\bar{B}C_i + \bar{A}B\bar{C}_i + A\bar{B}\bar{C}_i + ABC_i$$

$$= C_i(AB + \bar{A}\bar{B}) + \bar{C}_i(A\bar{B} + \bar{A}B)$$

$$= C_i(\overline{A \oplus B}) + \bar{C}_i(A \oplus B)$$

$$\therefore S = A \oplus B \oplus C$$

$$C_o = \Sigma 3, 5, 6, 7$$

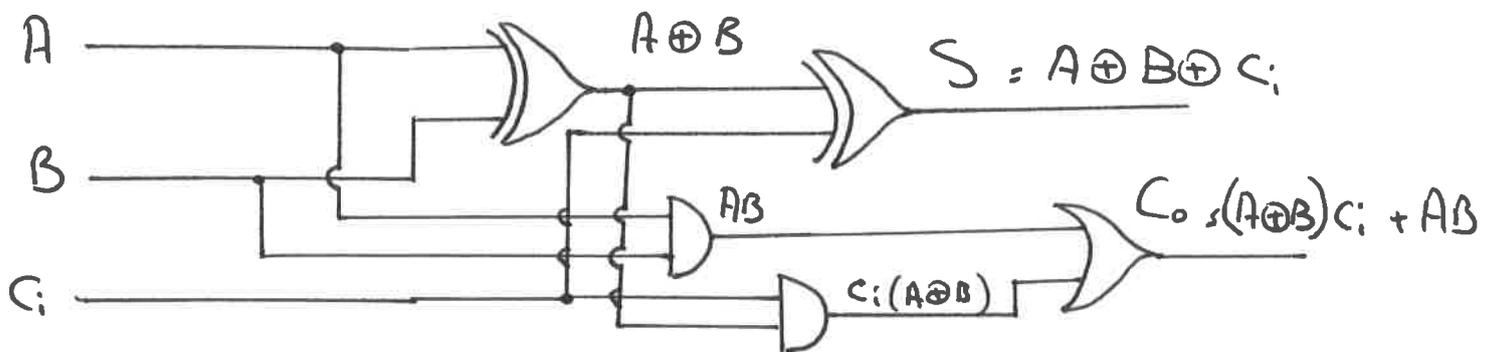
$$C_o = m_3 + m_5 + m_6 + m_7$$

$$= \bar{A}BC_i + A\bar{B}C_i + AB\bar{C}_i + ABC_i$$

$$= C_i(A\bar{B} + \bar{A}B) + AB$$

$$\therefore C_o = C_i(A \oplus B) + AB$$

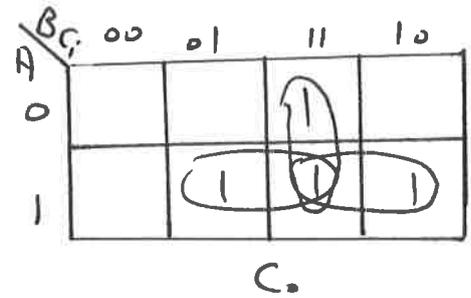
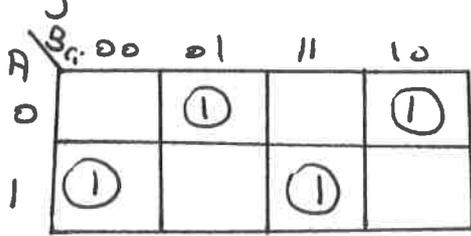
Logic cct



$$S = A \oplus B \oplus C$$

$$C_o = C_i(A \oplus B) + AB$$

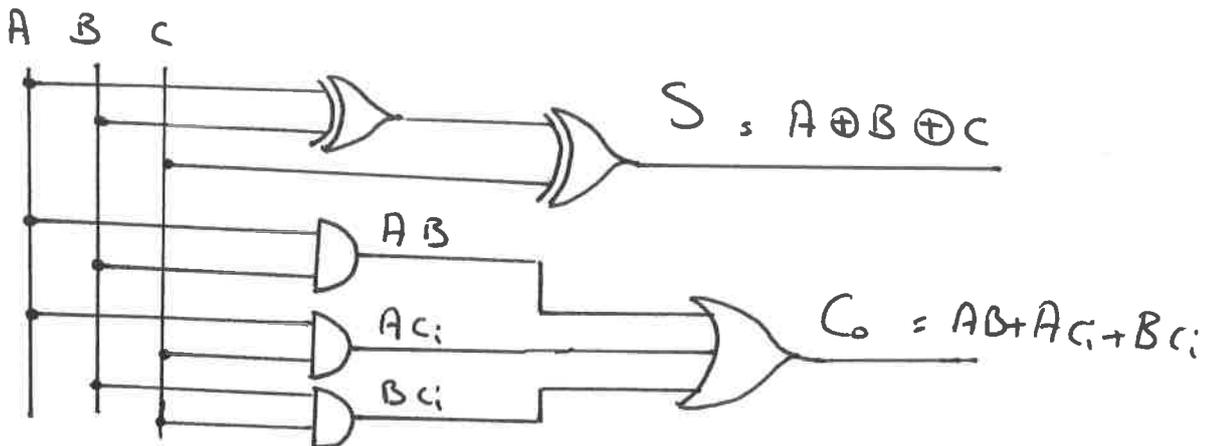
by using K-Map



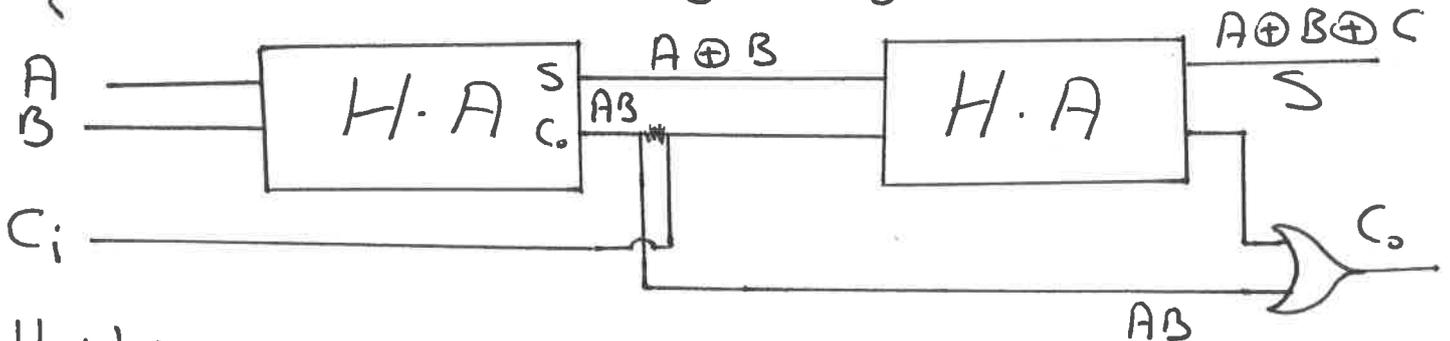
$$S = \bar{A}\bar{B}C_i + \bar{A}B\bar{C}_i + AB\bar{C}_i + A\bar{B}C_i$$

$$= A \oplus B \oplus C$$

$$C_o = AB + AC_i + BC_i$$



Ex) Build a Full-Adder by using two half-adder?



H.W :-

Ex) Build F.A by using NAND gate only?

Ex) Build F.A by using NOR gate only?

Ex) Design a Logic cct to provide an o/p of Logic (1) where every any two of three inputs are Logic (1)?

## Subtractors:-

A subtractors is a combinational circuit that subtract bits and produces their difference.

There are two types of Subtractors

① Half-Subtractor (H.S).

② Full-Subtractor (F.S).

### ① Half-Subtractor (H.S)

A half-Subtractor is a combinational circuit that subtract two bits and produces their difference.

The truth table

i/p		o/p	
A	B	D	B <sub>0</sub>
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0

where :-

D = Difference.

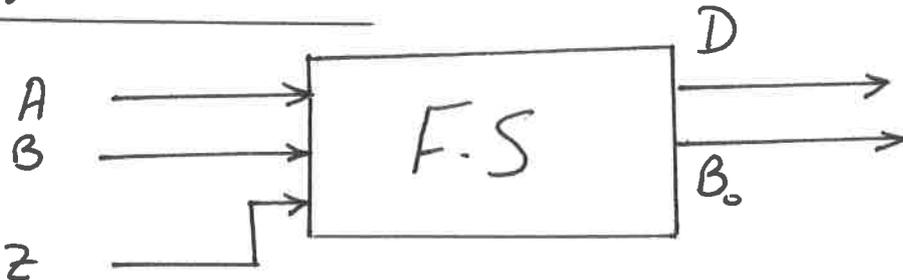
B<sub>0</sub> = Borrow.



Significant stages.

This cct has three input and two outputs.

Block-Diagram of (F.S)



The truth table

i/p			o/p	
A	B	z	D	B <sub>0</sub>
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

From truth table

$$D = \sum 1, 2, 4, 7$$

$$B_0 = \sum 1, 2, 3, 7$$

$$D = \bar{A}\bar{B}z + \bar{A}B\bar{z} + A\bar{B}\bar{z} + ABz$$

$$= z(\bar{A}\bar{B} + AB) + \bar{z}(A\bar{B} + \bar{A}B)$$

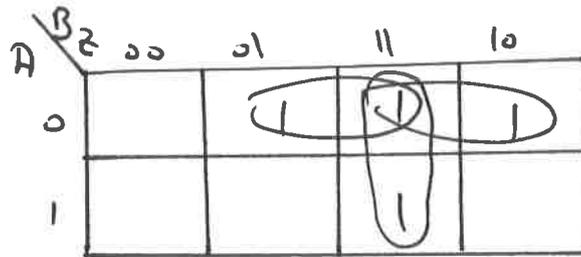
$$= z(A \oplus B) + \bar{z}(A \oplus B)$$

$$D = A \oplus B \oplus z$$

$$\begin{aligned}
 B_0 &= \bar{A}\bar{B}z + \bar{A}B\bar{z} + \bar{A}Bz + ABz \\
 &= z(\bar{A}\bar{B} + AB) + \bar{A}B(z + \bar{z}) \\
 &= z(\bar{A}\bar{B} + AB) + \bar{A}B \\
 &= z(\overline{A \oplus B}) + \bar{A}B
 \end{aligned}$$

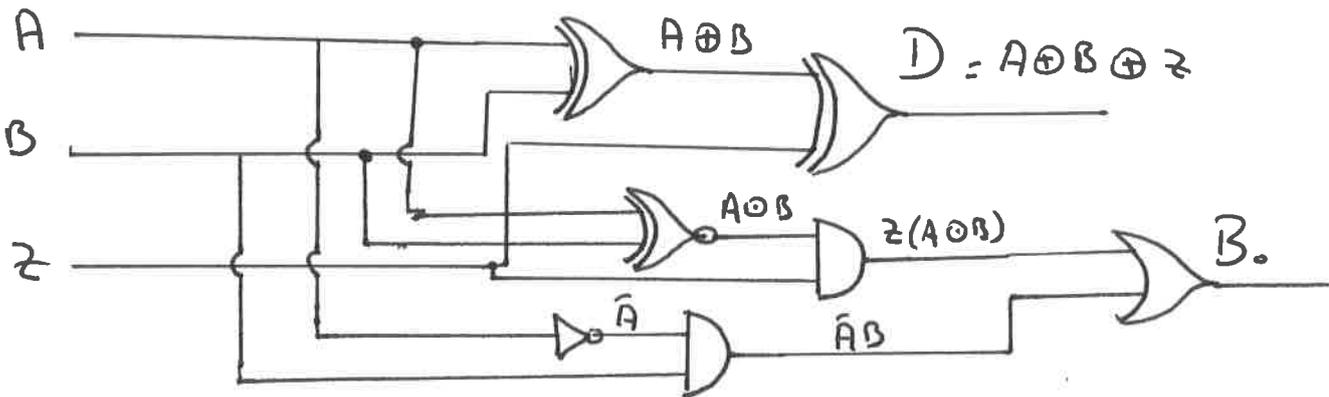
$$B_0 = z(A \odot B) + \bar{A}B$$

By using k-Map

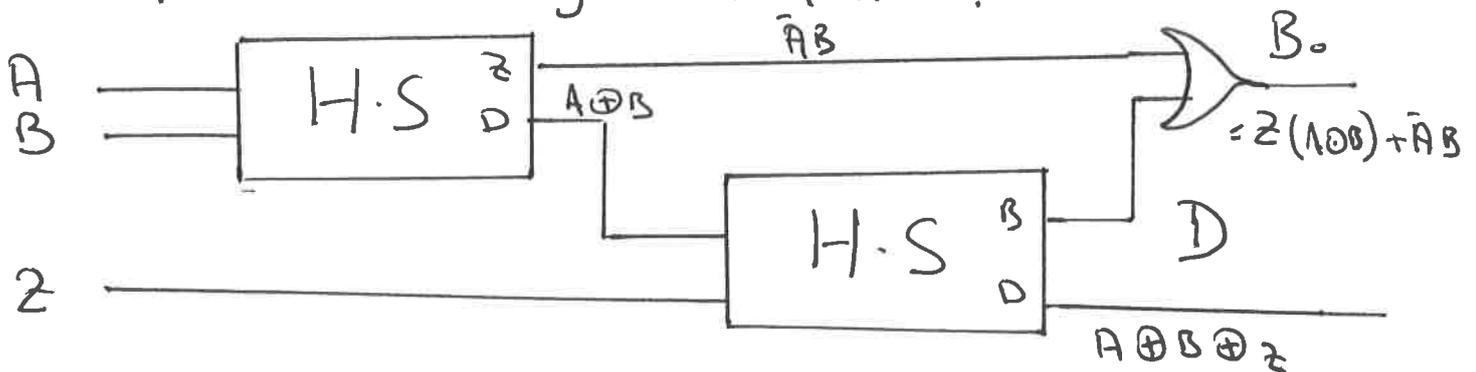


$$B_0 = \bar{A}B + \bar{A}z + Bz$$

The Logic cct



Ex) Implement a F.S by means of H.S ?



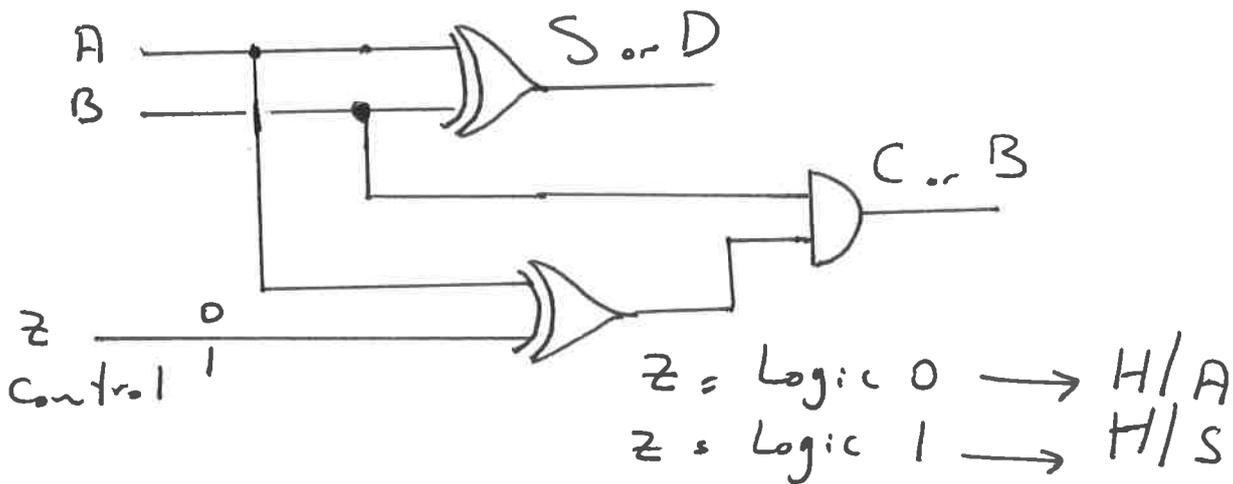
In H/A  $S = A \oplus B$

$C = AB$

In H/S  $D = A \oplus B$

$B = \bar{A}B$

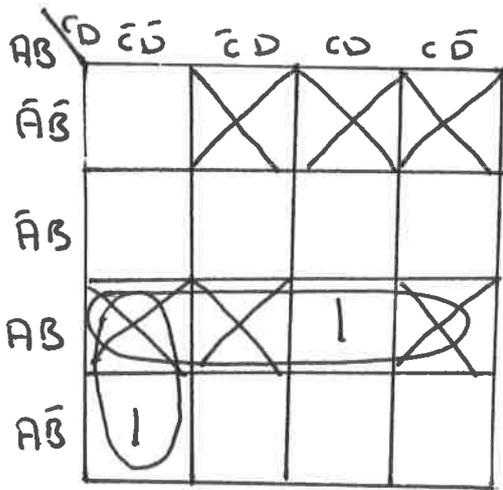
We can implement a Logic cct to (ADD or subtract), by using controller as follow: -



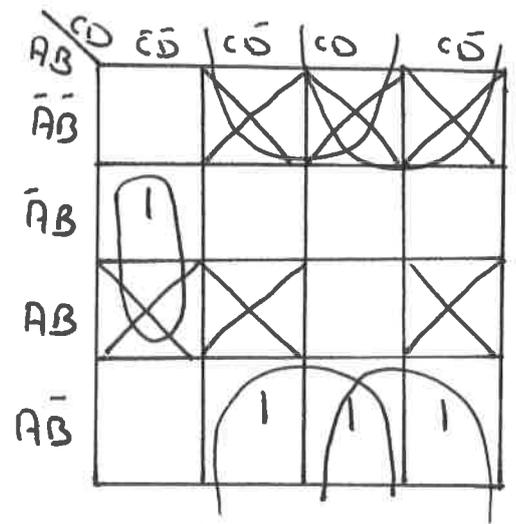
Ex) By mean's of Block diagram of H/A and two OR gates. Design a Logic cct that convert a decimal digit from the 84-2-1 code to BCD code?

i/p	8	4	-2	-1	o/p	w	x	y	z
A	B	C	D						
0	0	0	0		0	0	0	0	
0	1	1	1		0	0	0	1	
0	1	1	0		0	0	1	0	
0	1	0	1		0	0	1	1	
0	1	0	0		0	1	0	0	
1	0	1	1		0	1	0	1	
1	0	1	0		0	1	1	0	
1	0	0	1		0	1	1	1	
1	0	0	0		1	0	0	0	
1	1	1	1		1	0	0	1	

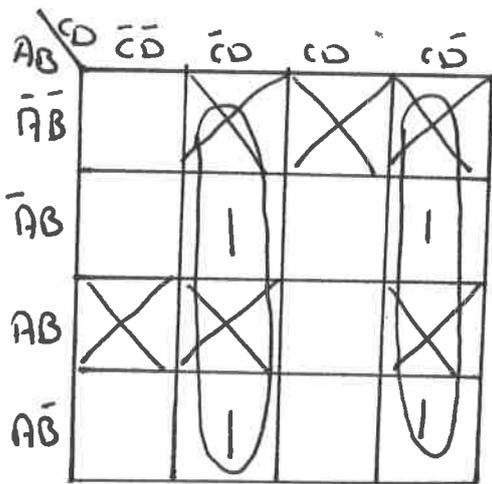
$w = \sum 8, 15$   
 $x = \sum 4, 11, 10, 9$   
 $y = \sum 6, 5, 10, 9$   
 $z = \sum 7, 5, 11, 9, 15$   
 $z = D$   
 don't care =  $\sum 1, 2, 3, 12, 13, 14$



$$W = AB + A\bar{C}\bar{D}$$

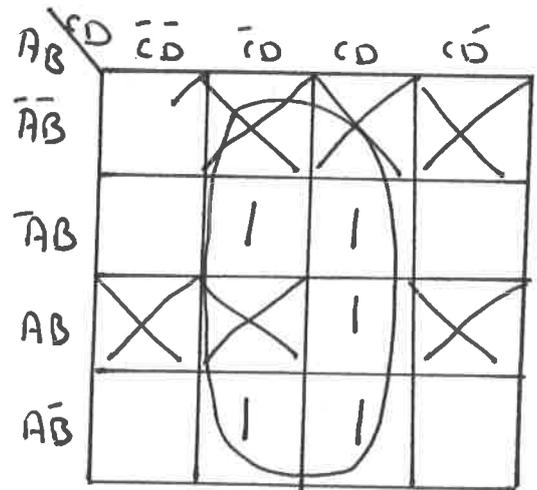


$$X' = B\bar{C}\bar{D} + \bar{B}D + \bar{B}C$$



$$Y = \bar{C}D + C\bar{D}$$

$$Y = A \oplus D$$



$$Z = D$$

